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# Hypergeometric0F0

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# Notations

### **Traditional name**

Generalized hypergeometric function  $_0F_0$ 

### **Traditional notation**

 $_0F_0(;\,;\,z)$ 

### Mathematica StandardForm notation

HypergeometricPFQ[{}, {}, {}]

# **Primary definition**

07.16.02.0001.01  $_0F_0(;;z) = \sum_{k=0}^{\infty} \frac{z^k}{k!} = e^z$ 

# Limit representations

$$07.16.09.0001.01$$
  

$${}_{0}F_{0}(; ; z) = \lim_{b \to \infty} {}_{0}F_{1}(; b; b z)$$
  

$$07.16.09.0002.01$$
  

$${}_{0}F_{0}(; ; z) = \lim_{a \to \infty} {}_{1}F_{0}\left(a; ; \frac{z}{a}\right)$$

# **Differential equations**

### Ordinary linear differential equations and wronskians

#### For the direct function itself

07.16.13.0001.01  $w'(z) - w(z) == 0 /; w(z) == c_{1 0}F_0(; ; z)$  07.16.13.0002.01 $w'(z) - w(z) == 0 /; w(z) == {}_0F_0(; ; z) \land w[0] == 1$ 

### Differentiation

### Low-order differentiation

 $\frac{07.16.20.0001.01}{\partial z_0 F_0(;;z)} = e^z$   $\frac{07.16.20.0002.01}{\partial z_0 F_0(;;z)}$   $\frac{\partial^2 {}_0 F_0(;;z)}{\partial z^2} = e^z$ 

### Symbolic differentiation

 $\frac{\partial^{n}{}_{0}F_{0}(;\,;\,z)}{\partial z^{n}} = e^{z} /; n \in \mathbb{N}$ 

# Fractional integro-differentiation

$$\frac{07.16.20.0004.01}{\partial {}^{\alpha}{}_{0}F_{0}(;;z)}{\partial z^{\alpha}} = e^{z} Q(-\alpha, 0, z)$$

# Integration

### Indefinite integration

Involving only one direct function

07.16.21.0001.01

$$\int_0 F_0(;;z) \, dz = e^z$$

Involving one direct function and elementary functions

Involving power function

$$\int z^{\alpha-1} {}_0F_0(;;z) \, dz = -(-z)^{-\alpha} \, z^{\alpha} \, \Gamma(\alpha,-z)$$

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